## Package 'smcfcs'

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**Title** Multiple Imputation of Covariates by Substantive Model Compatible Fully Conditional Specification

Version 1.9.2

URL https://github.com/jwb133/smcfcs

**Description** Implements multiple imputation of missing covariates by Substantive Model Compatible Fully Conditional Specification. This is a modification of the popular FCS/chained equations multiple imputation approach, and allows imputation of missing covariate values from models which are compatible with the user specified substantive model.

**Depends** R (>= 3.1.2)

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LazyData true

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Suggests knitr, rmarkdown, mitools, ggplot2, kmi, flexsurv

VignetteBuilder knitr

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ex\_cc

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## Description

A dataset containing simulated case cohort data, where the sub-cohort was a 10% random sample of the full cohort.

## Usage

ex\_cc

### **Format**

A data frame with 1571 rows and 7 variables:

- t Time to event or censoring
- **d** Indicator of whether event 1 occurred (d=1), or not (d=0)
- x Partially observed continuous covariate
- **z** Fully observed covariate

in.subco A binary indicator of whether the subject is in the sub-cohort

id An id variable

**entertime** The entry time variable to be used in the analysis

ex\_compet 3

ex_compet	Simulated example data with competing risks outcome and partially
	observed covariates

## Description

A dataset containing simulated competing risks data. There are two competing risks, and some times are also censored.

## Usage

ex\_compet

#### **Format**

A data frame with 1000 rows and 4 variables:

- t Time to event or censoring
- **d** Indicator of whether event 1 occurred (d=1), event 2 occurred (d=2) or individual was censored (d=0)
- x1 Partially observed binary covariate, with linear effects on log competing risk hazards
- x2 Partially observed normally distributed (conditional on x1) covariate, with linear effects on log competing risk hazards

ex_coxquad	Simulated example data with time to event outcome and quadratic covariate effects
	**

#### **Description**

A dataset containing simulated data where a time to event outcome depends quadratically on a partially observed covariate.

## Usage

ex\_coxquad

## **Format**

A data frame with 1000 rows and 6 variables:

- t Time to event or censoring
- d Binary indicator of whether event occurred or individual was censored
- **z** Fully observed covariate, with linear effect on outcome (on log hazard scale)

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 x Partially observed normally distributed covariate, with quadratic effect on outcome (on log hazard scale)

**xsq** The square of x, which thus has missing values also

v An auxiliary variable (i.e. not contained in the substantive model)

ex\_dtsam

Simulated discrete time survival data set

#### **Description**

A dataset containing simulated discrete time survival data.

## Usage

ex\_dtsam

#### **Format**

A data frame with 1000 rows and 8 variables:

- **x1** A binary variable with missing values
- x2 A fully observed continuous variable

failtime The discrete failure/censoring time

**d** Indicator of failure (=1) or censoring (=0)

ex\_finegray

Simulated example data with competing risks outcome and partially observed covariates

## **Description**

A dataset containing simulated competing risks data. There are two competing risks, and some times are also censored. Proportionality holds on the subdistribution hazard scale for cause 2, where for dataset 'ex\_compet' it instead holds on the cause-specific hazard scale.

#### Usage

ex\_finegray

ex\_flexsurv 5

#### **Format**

A data frame with 1000 rows and 4 variables:

times Time to event or censoring

**d** Indicator of whether event 1 occurred (d=1), event 2 occurred (d=2) or individual was censored (d=0)

- x1 Partially observed binary covariate, with linear effects on log subdistribution hazard of cause 1
- x2 Partially observed normally distributed (conditional on x1) covariate, with linear effects on log subdistribution hazard of cause 1

ex_flexsurv	Simulated example data with time-to-event Weibull outcome and two covariates

## Description

A dataset containing simulated data where the time-to-event outcome is Weibull distributed with two covariates, one of which is partially observed.

## Usage

ex\_flexsurv

#### **Format**

A data frame with 1000 rows and 4 variables:

- t Time to event (d=1) or censoring (d=0)
- d Event indicator
- x Partially observed binary covariate
- z Fully observed continuous covariate

ex_lininter	Simulated example data with continuous outcome and interaction be-
	tween two partially observed covariates

## **Description**

A dataset containing simulated data where the outcome depends on both main effects and interaction of two partially observed covariates.

#### Usage

ex\_lininter

6 ex\_logisticquad

#### **Format**

A data frame with 1000 rows and 4 variables:

- y Continuous outcome
- x1 Partially observed normally distributed covariate
- x2 Partially observed binary covariate

ex_linquad	Simulated example data with continuous outcome and quadratic co-
	variate effects

## **Description**

A dataset containing simulated data where the outcome depends quadratically on a partially observed covariate.

## Usage

ex\_linquad

#### **Format**

A data frame with 1000 rows and 5 variables:

- y Continuous outcome
- z Fully observed covariate, with linear effect on outcome
- x Partially observed normally distributed covariate, with quadratic effect on outcome
- **xsq** The square of x, which thus has missing values also
- v An auxiliary variable (i.e. not contained in the substantive model)

ex_logisticquad	Simulated example data with binary outcome and quadratic covariate effects
-----------------	--

## Description

A dataset containing simulated data where the binary outcome depends quadratically on a partially observed covariate.

## Usage

ex\_logisticquad

ex\_ncc 7

#### **Format**

A data frame with 1000 rows and 5 variables:

- y Binary outcome
- **z** Fully observed covariate, with linear effect on outcome (on log odds scale)
- x Partially observed normally distributed covariate, with quadratic effect on outcome (on log odds scale)

xsq The square of x, which thus has missing values also

v An auxiliary variable (i.e. not contained in the substantive model)

ex\_ncc

Simulated nested case-control data

## Description

A dataset containing simulated nested case-control data.

## Usage

ex\_ncc

#### **Format**

A data frame with 728 rows and 8 variables:

- t Time to event or censoring
- **d** Indicator of whether event 1 occurred (d=1), or not (d=0)
- x Partially observed binary covariate
- z Fully observed covariate
- id An id variable

numrisk Number of patients at risk at time of case's event

setno The case-control set number

**case** Binary indicator of case (=1) or control (=0)

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ex_poisson Simulated example data with count outcome, modelled using Poisson regression
---

## **Description**

A dataset containing simulated data where the count outcome depends on two covariates, x and z, with missing values in x. The substantive model is Poisson regression.

## Usage

```
ex_poisson
```

#### **Format**

A data frame with 1000 rows and 3 variables:

- y Count outcome
- z Fully observed covariate, with linear effect on outcome
- x Partially observed normally distributed covariate, with linear effect on outcome

plot.smcfcs Assess convergence of a smcfcs object

## Description

Visualises the contents of smCoefIter. Specifically, it plots the parameter estimates of the substantive model against the number of iterations from the imputation procedure. This is done for each regression coefficient, and each line corresponds to an imputed dataset.

#### Usage

```
## S3 method for class 'smcfcs'
plot(x, include = "all", ...)
```

## **Arguments**

An object of class 'smcfcs'

include

Character vector of coefficient names for which to return the convergence plot.

Default is "all" and returns plots for all coefficients in a facetted manner.

Recommendation is to plot first with include = "all", and then select coefficient names to zoom in to.

For competing risks, the coefficients are indexed by their cause. E.g. for coefficient of a variable x1 in a model for cause 2, will be labelled "x1-cause2".

Additional parameters to pass on to ggplot2::facet\_wrap(), eg. nrow = 2

#### **Details**

Requires loading of ggplot2 plotting library.

#### Value

A ggplot2 object, containing the convergence plots, facetted per covariate in the substantive model

## Author(s)

Edouard F. Bonneville <e.f.bonneville@lumc.nl>

## **Examples**

```
## Not run:
# Use simulated competing risks example in package
imps <- smcfcs(
    originaldata = ex_compet,
    smtype = "compet",
    smformula = list(
        "Surv(t, d == 1) ~ x1 + x2",
        "Surv(t, d == 2) ~ x1 + x2"
    ),
    method = c("", "", "norm", "norm")
)

plot(imps)
plot(imps, include = c("x1-cause1", "x2-cause2"))
## End(Not run)</pre>
```

smcfcs

Substantive model compatible fully conditional specification imputation of covariates.

## **Description**

Multiply imputes missing covariate values using substantive model compatible fully conditional specification.

## Usage

```
smcfcs(
  originaldata,
  smtype,
  smformula,
  method,
  predictorMatrix = NULL,
```

```
m = 5,
numit = 10,
rjlimit = 1000,
noisy = FALSE,
errorProneMatrix = NULL
)
```

#### **Arguments**

originaldata

The original data frame with missing values.

smtype

A string specifying the type of substantive model. Possible values are "lm", "logistic", "brlogistic", "poisson", "weibull", "coxph", "compet".

smformula

The formula of the substantive model. For "weibull" and "coxph" substantive models the left hand side should be of the form "Surv(t,d)". For "compet" substantive models, a list should be passed consisting of the Cox models for each cause of failure (see example).

method

A required vector of strings specifying for each variable either that it does not need to be imputed (""), the type of regression model to be be used to impute. Possible values are "norm" (normal linear regression), "logreg" (logistic regression), "brlogreg" (bias reduced logistic regression), "poisson" (Poisson regression), "podds" (proportional odds regression for ordered categorical variables), "mlogit" (multinomial logistic regression for unordered categorical variables), or a custom expression which defines a passively imputed variable, e.g. "x^2" or "x1\*x2". "latnorm" indicates the variable is a latent normal variable which is measured with error. If this is specified for a variable, the "errorProneMatrix" argument should also be used.

#### predictorMatrix

An optional predictor matrix. If specified, the matrix defines which covariates will be used as predictors in the imputation models (the outcome must not be included). The i'th row of the matrix should consist of 0s and 1s, with a 1 in the j'th column indicating the j'th variable be used as a covariate when imputing the i'th variable. If not specified, when imputing a given variable, the imputation model covariates are the other covariates of the substantive model which are partially observed (but which are not passively imputed) and any fully observed covariates (if present) in the substantive model. Note that the outcome variable is implicitly conditioned on by the rejection sampling scheme used by smcfcs, and should not be specified as a predictor in the predictor matrix.

 $\mathsf{m}$ 

The number of imputed datasets to generate. The default is 5.

numit

The number of iterations to run when generating each imputation. In a (limited) range of simulations good performance was obtained with the default of 10 iterations. However, particularly when the proportion of missingness is large, more iterations may be required for convergence to stationarity.

rjlimit

Specifies the maximum number of attempts which should be made when using rejection sampling to draw from imputation models. If the limit is reached when running a warning will be issued. In this case it is probably advisable to increase the rjlimit until the warning does not appear.

noisy

logical value (default FALSE) indicating whether output should be noisy, which can be useful for debugging or checking that models being used are as desired.

errorProneMatrix

An optional matrix which if specified indicates that some variables are measured with classical measurement error. If the i'th variable is measured with error by variables j and k, then the (i,j) and (i,k) entries of this matrix should be 1, with the remainder of entries 0. The i'th element of the method argument should then be specified as "latnorm". See the measurement error vignette for more details.

#### **Details**

smcfcs imputes missing values of covariates using the Substantive Model Compatible Fully Conditional Specification multiple imputation approach proposed by Bartlett *et al* 2015 (see references).

Imputation is supported for linear regression ("lm"), logistic regression ("logistic"), bias reduced logistic regression ("brlogistic"), Poisson regression ("poisson"), Weibull ("weibull") and Cox regression for time to event data ("coxph"), and Cox models for competing risks data ("compet"). For "coxph", the event indicator should be integer coded with 0 for censoring and 1 for event. For "compet", a Cox model is assumed for each cause specific hazard function, and the event indicator should be integer coded with 0 corresponding to censoring, 1 corresponding to failure from the first cause etc.

The function returns a list. The first element impDataset of the list is a list of the imputed datasets. Models (e.g. the substantive model) can be fitted to each and results combined using Rubin's rules using the mitools package, as illustrated in the examples.

The second element smCoefIter is a three dimensional array containing the values of the substantive model parameters obtained at the end of each iteration of the algorithm. The array is indexed by: imputation number, parameter number, iteration.

If the substantive model is linear, logistic or Poisson regression, smcfcs will automatically impute missing outcomes, if present, using the specified substantive model. However, even in this case, the user should specify "" in the element of method corresponding to the outcome variable.

The bias reduced methods make use of the <code>brglm2</code> package to fit the corresponding glms using Firth's bias reduced approach. These may be particularly useful to use in case of perfect prediction, since the resulting model estimates are always guaranteed to be finite, even in the case of perfect prediction.

The development of this package was supported by the UK Medical Research Council (Fellowship MR/K02180X/1 and grant MR/T023953/1). Part of its development took place while Bartlett was kindly hosted by the University of Michigan's Department of Biostatistics & Institute for Social Research.

The structure of many of the arguments to smcfcs are based on those of the excellent mice package.

#### Value

A list containing:

impDatasets a list containing the imputed datasets

smCoefIter a three dimension matrix containing the substantive model parameter values. The matrix is indexed by [imputation,parameter number,iteration]

#### Author(s)

Jonathan Bartlett < jonathan.bartlett1@lshtm.ac.uk>

#### References

Bartlett JW, Seaman SR, White IR, Carpenter JR. Multiple imputation of covariates by fully conditional specification: accommodating the substantive model. Statistical Methods in Medical Research 2015; 24(4): 462-487. doi:10.1177/0962280214521348

#### **Examples**

```
#set random number seed to make results reproducible
set.seed(123)
#linear substantive model with quadratic covariate effect
imps <- smcfcs(ex_linguad, smtype="lm", smformula="y~z+x+xsq",</pre>
               method=c("","","norm","x^2",""))
#if mitools is installed, fit substantive model to imputed datasets
#and combine results using Rubin's rules
if (requireNamespace("mitools", quietly = TRUE)) {
 library(mitools)
 impobj <- imputationList(imps$impDatasets)</pre>
 models <- with(impobj, lm(y^z+x+xsq))
 summary(MIcombine(models))
}
#the following examples are not run when the package is compiled on CRAN
#(to keep computation time down), but they can be run by package users
## Not run:
 #examining convergence, using 100 iterations, setting m=1
 imps <- smcfcs(ex_linguad, smtype="lm", smformula="y~z+x+xsq",</pre>
                 method=c("","","norm","x^2",""),m=1,numit=100)
 #convergence plot from first imputation for third coefficient of substantive model
 plot(imps$smCoefIter[1,3,])
 #include auxiliary variable assuming it is conditionally independent of Y (which it is here)
 predMatrix <- array(0, dim=c(ncol(ex_linquad),ncol(ex_linquad)))</pre>
 predMatrix[3,] \leftarrow c(0,1,0,0,1)
 imps <- smcfcs(ex_linguad, smtype="lm", smformula="y~z+x+xsq",</pre>
                 method=c("","","norm","x^2",""),predictorMatrix=predMatrix)
 #impute missing x1 and x2, where they interact in substantive model
 imps <- smcfcs(ex_lininter, smtype="lm", smformula="y~x1+x2+x1*x2",</pre>
                 method=c("","norm","logreg"))
 #logistic regression substantive model, with quadratic covariate effects
  imps <- smcfcs(ex_logisticquad, smtype="logistic", smformula="y~z+x+xsq",</pre>
                 method=c("","","norm","x^2",""))
 #Poisson regression substantive model
  imps <- smcfcs(ex_poisson, smtype="poisson", smformula="y~x+z",</pre>
```

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```
method=c("","norm",""))
 if (requireNamespace("mitools", quietly = TRUE)) {
   library(mitools)
    impobj <- imputationList(imps$impDatasets)</pre>
   models <- with(impobj, glm(y~x+z,family=poisson))</pre>
   summary(MIcombine(models))
 }
 #Cox regression substantive model, with only main covariate effects
 if (requireNamespace("survival", quietly = TRUE)) {
    imps <- smcfcs(ex_coxquad, smtype="coxph", smformula="Surv(t,d)~z+x+xsq",
                   method=c("","","","norm","x^2",""))
    #competing risks substantive model, with only main covariate effects
    imps <- smcfcs(ex_compet, smtype="compet",</pre>
                   smformula=c("Surv(t,d==1)~x1+x2", "Surv(t,d==2)~x1+x2"),
                   method=c("","","logreg","norm"))
 }
 #if mitools is installed, fit model for first competing risk
 if (requireNamespace("mitools", quietly = TRUE)) {
    library(mitools)
    impobj <- imputationList(imps$impDatasets)</pre>
   models <- with(impobj, coxph(Surv(t,d==1)^x1+x2))
   summary(MIcombine(models))
 #discrete time survival analysis example
 M <- 5
 imps <- smcfcs(ex_dtsam, "dtsam", "Surv(failtime,d)~x1+x2",</pre>
                 method=c("logreg","", "", ""),m=M)
 #fit dtsam model to each dataset manually, since we need
 #to expand to person-period data form first
 ests <- vector(mode = "list", length = M)</pre>
 vars <- vector(mode = "list", length = M)</pre>
 for (i in 1:M) {
    longData <- survSplit(Surv(failtime,d)~x1+x2, data=imps$impDatasets[[i]],</pre>
                           cut=unique(ex_dtsam$failtime[ex_dtsam$d==1]))
   mod <- glm(d~-1+factor(tstart)+x1+x2, family="binomial", data=longData)</pre>
   ests[[i]] <- coef(mod)</pre>
    vars[[i]] <- diag(vcov(mod))</pre>
 summary(MIcombine(ests,vars))
## End(Not run)
```

smcfcs.casecohort

Substantive model compatible fully conditional specification imputation of covariates for case cohort studies 14 smcfcs.casecohort

#### **Description**

Multiply imputes missing covariate values using substantive model compatible fully conditional specification for case cohort studies.

#### Usage

```
smcfcs.casecohort(
  originaldata,
  smformula,
  sampfrac,
  in.subco,
  method,
  predictorMatrix = NULL,
  m = 5,
  numit = 10,
  rjlimit = 1000,
  noisy = FALSE,
  errorProneMatrix = NULL
)
```

#### **Arguments**

originaldata

The case-cohort data set (NOT a full cohort data set with a case-cohort substudy within it)

smformula

A formula of the form "Surv(entertime,t,d)~x", where d is the event (d=1) or censoring (d=0) indicator, t is the event or censoring time and entertime is equal to the time origin (typically 0) for individuals in the subcohort and is equal to (t-0.001) for cases outside the subcohort [this sets cases outside the subcohort to enter follow-up just before their event time. The value 0.001 may need to be modified depending on the time scale.]

sampfrac

The proportion of individuals from the underlying full cohort who are in the subcohort

in.subco

The name of a column in the dataset with 0/1s that indicates whether the subject is in the subcohort

method

A required vector of strings specifying for each variable either that it does not need to be imputed (""), the type of regression model to be be used to impute. Possible values are "norm" (normal linear regression), "logreg" (logistic regression), "brlogreg" (bias reduced logistic regression), "poisson" (Poisson regression), "podds" (proportional odds regression for ordered categorical variables), "mlogit" (multinomial logistic regression for unordered categorical variables), or a custom expression which defines a passively imputed variable, e.g. "x^2" or "x1\*x2". "latnorm" indicates the variable is a latent normal variable which is measured with error. If this is specified for a variable, the "errorProneMatrix" argument should also be used.

#### predictorMatrix

An optional predictor matrix. If specified, the matrix defines which covariates will be used as predictors in the imputation models (the outcome must not be

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included). The i'th row of the matrix should consist of 0s and 1s, with a 1 in the j'th column indicating the j'th variable be used as a covariate when imputing the i'th variable. If not specified, when imputing a given variable, the imputation model covariates are the other covariates of the substantive model which are partially observed (but which are not passively imputed) and any fully observed covariates (if present) in the substantive model. Note that the outcome variable is implicitly conditioned on by the rejection sampling scheme used by smcfcs, and should not be specified as a predictor in the predictor matrix.

The number of imputed datasets to generate. The default is 5.

numit The number of iterations to run when generating each imputation. In a (limited)

range of simulations good performance was obtained with the default of 10 iterations. However, particularly when the proportion of missingness is large, more

iterations may be required for convergence to stationarity.

rjlimit Specifies the maximum number of attempts which should be made when using

rejection sampling to draw from imputation models. If the limit is reached when running a warning will be issued. In this case it is probably advisable to increase

the rjlimit until the warning does not appear.

noisy logical value (default FALSE) indicating whether output should be noisy, which

can be useful for debugging or checking that models being used are as desired.

errorProneMatrix

An optional matrix which if specified indicates that some variables are measured with classical measurement error. If the i'th variable is measured with error by variables j and k, then the (i,j) and (i,k) entries of this matrix should be 1, with the remainder of entries 0. The i'th element of the method argument should then be specified as "latnorm". See the measurement error vignette for more details.

#### Details

This version of smcfcs is designed for use with case cohort studies but where the analyst does not wish to, or cannot (due to not having the necessary data) impute the full cohort. The function's arguments are the same as for the main smcfcs function, except for smformula, in.subco, and sampfrac - see above for details on how these should be specified.

#### Author(s)

```
Ruth Keogh <ruth.keogh@lshtm.ac.uk>
Jonathan Bartlett <jonathan.bartlett1@lshtm.ac.uk>
```

#### **Examples**

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```
models <- with(impobj, coxph(Surv(entertime,t,d)~x+z+cluster(id)))
summary(MIcombine(models))
## End(Not run)</pre>
```

smcfcs.dtsam

Substantive model compatible fully conditional specification imputation of covariates for discrete time survival analysis

## Description

Multiply imputes missing covariate values using substantive model compatible fully conditional specification for discrete time survival analysis.

#### Usage

```
smcfcs.dtsam(
  originaldata,
  smformula,
  timeEffects = "factor",
  method,
  predictorMatrix = NULL,
  m = 5,
  numit = 10,
  rjlimit = 1000,
  noisy = FALSE,
  errorProneMatrix = NULL
)
```

### **Arguments**

originaldata The data in wide form (i.e. one row per subject)

smformula A formula of the form "Surv $(t,d) \sim x1+x2+x3$ ", where t is the discrete time vari-

able, d is the binary event indicator, and the covariates should not include time. The time variable should be an integer coded numeric variable taking values

from 1 up to the final time period.

timeEffects Specifies how the effect of time is modelled. timeEffects="factor" (the de-

fault) models time as a factor variable. timeEffects="linear" and timeEffects="quad"

specify that time be modelled as a continuous linear or quadratic effect on the

log odds scale respectively.

method A required vector of strings specifying for each variable either that it does not

need to be imputed (""), the type of regression model to be be used to impute. Possible values are "norm" (normal linear regression), "logreg" (logistic regression), "brlogreg" (bias reduced logistic regression), "poisson" (Poisson regression), "podds" (proportional odds regression for ordered categorical variables), "mlogit" (multinomial logistic regression for unordered categorical

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> variables), or a custom expression which defines a passively imputed variable, e.g. "x^2" or "x1\*x2". "latnorm" indicates the variable is a latent normal variable which is measured with error. If this is specified for a variable, the "errorProneMatrix" argument should also be used.

#### predictorMatrix

An optional predictor matrix. If specified, the matrix defines which covariates will be used as predictors in the imputation models (the outcome must not be included). The i'th row of the matrix should consist of 0s and 1s, with a 1 in the j'th column indicating the j'th variable be used as a covariate when imputing the i'th variable. If not specified, when imputing a given variable, the imputation model covariates are the other covariates of the substantive model which are partially observed (but which are not passively imputed) and any fully observed covariates (if present) in the substantive model. Note that the outcome variable is implicitly conditioned on by the rejection sampling scheme used by smcfcs, and should not be specified as a predictor in the predictor matrix.

The number of imputed datasets to generate. The default is 5.

The number of iterations to run when generating each imputation. In a (limited) range of simulations good performance was obtained with the default of 10 iterations. However, particularly when the proportion of missingness is large, more

iterations may be required for convergence to stationarity.

Specifies the maximum number of attempts which should be made when using rejection sampling to draw from imputation models. If the limit is reached when running a warning will be issued. In this case it is probably advisable to increase

the rjlimit until the warning does not appear.

logical value (default FALSE) indicating whether output should be noisy, which

can be useful for debugging or checking that models being used are as desired.

errorProneMatrix

An optional matrix which if specified indicates that some variables are measured with classical measurement error. If the i'th variable is measured with error by variables j and k, then the (i,j) and (i,k) entries of this matrix should be 1, with the remainder of entries 0. The i'th element of the method argument should then be specified as "latnorm". See the measurement error vignette for more details.

## **Details**

For this substantive model type, like for the other substantive model types, smcfcs expects the original data to have one row per subject. Variables indicating the discrete time of failure/censoring and the event indicator should be passed in smformula, as described.

The default is to model the effect of time as a factor. This will not work in datasets where there is not at least one observed event in each time period. In such cases you must specify a simpler parametric model for the effect of time. At the moment you can specify either a linear or quadratic effect of time (on the log odds scale).

#### Author(s)

Jonathan Bartlett < jonathan.bartlett1@lshtm.ac.uk>

m

numit

rjlimit

noisy

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## **Examples**

```
#the following example is not run when the package is compiled on CRAN
#(to keep computation time down), but it can be run by package users
## Not run:
 #discrete time survival analysis example
 M < -5
 imps <- smcfcs.dtsam(ex_dtsam, "Surv(failtime,d)~x1+x2",</pre>
                  method=c("logreg","", "", ""),m=M)
 #fit dtsam model to each dataset manually, since we need
 #to expand to person-period data form first
 ests <- vector(mode = "list", length = M)</pre>
 vars <- vector(mode = "list", length = M)</pre>
 for (i in 1:M) {
    longData <- survSplit(Surv(failtime,d)~x1+x2, data=imps$impDatasets[[i]],</pre>
                           cut=unique(ex_dtsam$failtime[ex_dtsam$d==1]))
    mod <- glm(d~-1+factor(tstart)+x1+x2, family="binomial", data=longData)</pre>
   ests[[i]] <- coef(mod)</pre>
    vars[[i]] <- diag(vcov(mod))</pre>
 library(mitools)
 summary(MIcombine(ests, vars))
## End(Not run)
```

smcfcs.finegray

Substantive model compatible fully conditional specification imputation of covariates for a Fine-Gray model

## Description

Multiply imputes missing covariate values using substantive model compatible fully conditional specification for competing risks outcomes, when the substantive model is a Fine-Gray model for the subdistribution hazard of one event.

### Usage

```
smcfcs.finegray(
  originaldata,
  smformula,
  method,
  cause = 1,
  m = 5,
  numit = 10,
  rjlimit = 5000,
  kmi_args = list(formula = ~1, bootstrap = FALSE, nboot = 10),
  ...
)
```

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#### **Arguments**

original data frame with missing values.

smformula The formula of the substantive model, given as a string. Needs to be of the

form "Surv(t, d)  $\sim$  x1 + x2", where t is a vector of competing event times, and d is a (numeric) competing event indicator, where 0 must designate a censored

observation.

method A required vector of strings specifying for each variable either that it does not

need to be imputed (""), the type of regression model to be be used to impute. Possible values are "norm" (normal linear regression), "logreg" (logistic regression), "brlogreg" (bias reduced logistic regression), "poisson" (Poisson regression), "podds" (proportional odds regression for ordered categorical variables), "mlogit" (multinomial logistic regression for unordered categorical variables), or a custom expression which defines a passively imputed variable, e.g. "x^2" or "x1\*x2". "latnorm" indicates the variable is a latent normal variable which is measured with error. If this is specified for a variable, the

"errorProneMatrix" argument should also be used.

cause Numeric, designating the competing event of interest (default is 'cause = 1').

m The number of imputed datasets to generate. The default is 5.

numit The number of iterations to run when generating each imputation. In a (limited)

range of simulations good performance was obtained with the default of 10 iterations. However, particularly when the proportion of missingness is large, more

iterations may be required for convergence to stationarity.

rjlimit Specifies the maximum number of attempts which should be made when using

rejection sampling to draw from imputation models. If the limit is reached when running a warning will be issued. In this case it is probably advisable to increase

the rjlimit until the warning does not appear.

kmi\_args List, containing arguments to be passed on to kmi. The "formula" element is

a formula where the right-hand side specifies the covariates used for multiply imputing the potential censoring times for individual's failing from competing events. The default is 'formula =  $\sim 1$ ', which uses marginal Kaplan-Meier esti-

mator of the censoring distribution.

... Additional arguments to pass on to smcfcs

#### **Details**

In the presence of random right censoring, the function first multiply imputes the potential censoring times for those failing from competing events using kmi, and thereafter uses smcfcs to impute the missing covariates. See Bonneville *et al.* 2024 for further details on the methodology.

The function does not (yet) support parallel computation.

#### Value

An object of type "smcfcs", as would usually be returned from smcfcs.

## Author(s)

Edouard F. Bonneville <e.f.bonneville@lumc.nl>

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#### References

Bonneville EF, Beyersmann J, Keogh RH, Bartlett JW, Morris TP, Polverelli N, de Wreede LC, Putter H. Multiple imputation of missing covariates when using the Fine–Gray model. 2024. Submitted.

#### **Examples**

```
## Not run:
library(survival)
library(kmi)
imps <- smcfcs.finegray(</pre>
  originaldata = ex_finegray,
  smformula = "Surv(times, d) \sim x1 + x2",
  method = c("", "", "logreg", "norm"),
  cause = 1,
  kmi_args = list("formula" = ~ 1)
)
if (requireNamespace("mitools", quietly = TRUE)) {
  library(mitools)
  impobj <- imputationList(imps$impDatasets)</pre>
  # Important: use Surv(newtimes, newevent) ~ ... when pooling
  # (respectively: subdistribution time and indicator for cause of interest)
  models <- with(impobj, coxph(Surv(newtimes, newevent) ~ x1 + x2))</pre>
  summary(MIcombine(models))
}
## End(Not run)
```

smcfcs.flexsurv

Substantive model compatible fully conditional specification imputation of covariates and event times using flexible parametric survival models

#### **Description**

Multiply imputes missing covariate values and event times using substantive model compatible fully conditional specification with a Royston-Parmar flexible parametric survival model.

## Usage

```
smcfcs.flexsurv(
  originaldata,
  smformula,
  k = 2,
  imputeTimes = FALSE,
  censtime = NULL,
```

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```
originalKnots = TRUE,
method,
predictorMatrix = NULL,
m = 5,
numit = 10,
rjlimit = 1000,
noisy = FALSE,
errorProneMatrix = NULL)
```

#### **Arguments**

original data frame with missing values.

smformula A formula of the form "Surv $(t,d)\sim x+z$ "

k Number of knots to use in the flexible parametric survival model

imputeTimes If set to TRUE, smcfcs.flexsurv will impute censored survival times, as well

as any missing covariates

censtime Value(s) to use for censoring of imputed event times. If a vector, it should be of

length equal to the number of original censored individuals

originalKnots If imputing censored event times, setting originalKnots=TRUE means the au-

tomatically chosen knot locations from the model fitted to the observed times are used throughout. If FALSE, knots are chosen automatically at each iteration by flexsurvspline based on the current observed+imputed event times,

according to the chosen value of k.

method A required vector of strings specifying for each variable either that it does not

need to be imputed (""), the type of regression model to be be used to impute. Possible values are "norm" (normal linear regression), "logreg" (logistic regression), "brlogreg" (bias reduced logistic regression), "poisson" (Poisson regression), "podds" (proportional odds regression for ordered categorical variables), "mlogit" (multinomial logistic regression for unordered categorical variables), or a custom expression which defines a passively imputed variable, e.g. "x^2" or "x1\*x2". "latnorm" indicates the variable is a latent normal variable which is measured with error. If this is specified for a variable, the

"errorProneMatrix" argument should also be used.

predictorMatrix

An optional predictor matrix. If specified, the matrix defines which covariates will be used as predictors in the imputation models (the outcome must not be included). The i'th row of the matrix should consist of 0s and 1s, with a 1 in the j'th column indicating the j'th variable be used as a covariate when imputing the i'th variable. If not specified, when imputing a given variable, the imputation model covariates are the other covariates of the substantive model which are partially observed (but which are not passively imputed) and any fully observed covariates (if present) in the substantive model. Note that the outcome variable is implicitly conditioned on by the rejection sampling scheme used by smcfcs, and should not be specified as a predictor in the predictor matrix.

The number of imputed datasets to generate. The default is 5.

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numit The number of iterations to run when generating each imputation. In a (limited)

range of simulations good performance was obtained with the default of 10 iterations. However, particularly when the proportion of missingness is large, more

iterations may be required for convergence to stationarity.

rjlimit Specifies the maximum number of attempts which should be made when using

rejection sampling to draw from imputation models. If the limit is reached when running a warning will be issued. In this case it is probably advisable to increase

the rjlimit until the warning does not appear.

noisy logical value (default FALSE) indicating whether output should be noisy, which

can be useful for debugging or checking that models being used are as desired.

errorProneMatrix

An optional matrix which if specified indicates that some variables are measured with classical measurement error. If the i'th variable is measured with error by variables j and k, then the (i,j) and (i,k) entries of this matrix should be 1, with the remainder of entries 0. The i'th element of the method argument should then be specified as "latnorm". See the measurement error vignette for more details.

#### **Details**

This version of smcfcs is for time-to-event outcomes which are modelled using a flexible parametric proportional hazards survival model, as proposed by Royston and Parmar (2002). The model is fitted using the flexsurvspline function in the flexsurv package. Specifically it fits models using the hazard scale. The flexibility of the model can be changed by modifying the k argument, which specifies the number of knots.

If desired, smcfcs.flexsurv can be used to impute event times for individuals who are originally censored, by specifying imputeTimes=TRUE. In the resulting imputed datasets every individual will have an event time and the event indicator will be one for all. Alternatively, you can impute censored times, but setting a larger potential censoring time, which is either a common value used for all or a vector of times, by using the censtime argument. If some individuals have their time-to-event outcome completely missing and you want to impute this, they should have a time of zero and the event indicator set to zero.

flexsurvspline sometimes fails during model fitting. If/when this occurs, smcfcs.flexsurv takes a posterior draw based on the model fit from the preceding iteration, and a warning is printed at the end of the smcfcs.flexsurv run detailing how many times it occurred.

## Author(s)

Jonathan Bartlett < jonathan.bartlett1@lshtm.ac.uk>

#### References

Royston P, Parmar MKB. Flexible parametric proportional-hazards and proportional-odds models for censored survival data, with application to prognostic modelling and estimation of treatment effects. Statistics in Medicine 2002; 21(15): 2175-2197. doi:10.1002/sim.1203

#### **Examples**

#the following example is not run when the package is compiled on CRAN

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```
#(to keep computation time down), but it can be run by package users
   set.seed(63213)
   imps <- smcfcs.flexsurv(ex_flexsurv,</pre>
                             smformula="Surv(t,d)~x+z",
                             method=c("","","logreg",""))
   library(mitools)
   impobj <- imputationList(imps$impDatasets)</pre>
   models <- with(impobj, flexsurvspline(Surv(t,d)^x+z, k=2))
   summary(MIcombine(models))
   # now impute event times as well as missing covariates
   imps <- smcfcs.flexsurv(ex_flexsurv,</pre>
                             k=2,
                             smformula="Surv(t,d)~x+z",
                             method=c("","","logreg",""),
                             imputeTimes=TRUE)
   # now impute event times as well as missing covariates,
   # but setting max observed event time to 2
   imps <- smcfcs.flexsurv(ex_flexsurv,</pre>
                             k=2,
                             smformula="Surv(t,d)~x+z",
                             method=c("","","logreg",""),
                             imputeTimes=TRUE,
                             censtime=2)
 ## End(Not run)
smcfcs.nestedcc
                          Substantive model compatible fully conditional specification imputa-
```

## **Description**

Multiply imputes missing covariate values using substantive model compatible fully conditional specification for nested case control studies.

tion of covariates for nested case control studies

## Usage

```
smcfcs.nestedcc(
  originaldata,
  smformula,
  set,
  event,
  nrisk,
```

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```
method,
predictorMatrix = NULL,
m = 5,
numit = 10,
rjlimit = 1000,
noisy = FALSE,
errorProneMatrix = NULL
)
```

#### **Arguments**

substudy within it)

smformula A formula of the form "Surv(t,case)~x+strata(set)", where case is case-control

indicator, t is the event or censoring time. Note that t could be set to the case's event time for the matched controls in a given set. The right hand side should

include the case control set as a strata term (see example).

set variable identifying matched sets in nested case-control study

event variable which indicates who is a case/control in the nested case-control sample.

Note that this is distinct from d.

nrisk variable which is the number at risk (in the underlying full cohort) at the event

time for the case in each matched set (i.e. nrisk is the same for all individuals in

a matched set).

method A required vector of strings specifying for each variable either that it does not

need to be imputed (""), the type of regression model to be be used to impute. Possible values are "norm" (normal linear regression), "logreg" (logistic regression), "brlogreg" (bias reduced logistic regression), "poisson" (Poisson regression), "podds" (proportional odds regression for ordered categorical variables), "mlogit" (multinomial logistic regression for unordered categorical variables), or a custom expression which defines a passively imputed variable, e.g. "x^2" or "x1\*x2". "latnorm" indicates the variable is a latent normal variable which is measured with error. If this is specified for a variable, the

"errorProneMatrix" argument should also be used.

predictorMatrix

m

An optional predictor matrix. If specified, the matrix defines which covariates will be used as predictors in the imputation models (the outcome must not be included). The i'th row of the matrix should consist of 0s and 1s, with a 1 in the j'th column indicating the j'th variable be used as a covariate when imputing the i'th variable. If not specified, when imputing a given variable, the imputation model covariates are the other covariates of the substantive model which are partially observed (but which are not passively imputed) and any fully observed covariates (if present) in the substantive model. Note that the outcome variable is implicitly conditioned on by the rejection sampling scheme used by smcfcs, and should not be specified as a predictor in the predictor matrix.

The number of imputed datasets to generate. The default is 5.

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numit The number of iterations to run when generating each imputation. In a (limited)

range of simulations good performance was obtained with the default of 10 iterations. However, particularly when the proportion of missingness is large, more

iterations may be required for convergence to stationarity.

rjlimit Specifies the maximum number of attempts which should be made when using

rejection sampling to draw from imputation models. If the limit is reached when running a warning will be issued. In this case it is probably advisable to increase

the rjlimit until the warning does not appear.

noisy logical value (default FALSE) indicating whether output should be noisy, which

can be useful for debugging or checking that models being used are as desired.

errorProneMatrix

An optional matrix which if specified indicates that some variables are measured with classical measurement error. If the i'th variable is measured with error by variables j and k, then the (i,j) and (i,k) entries of this matrix should be 1, with the remainder of entries 0. The i'th element of the method argument should then be specified as "latnorm". See the measurement error vignette for more details.

#### **Details**

This version of smcfcs is designed for use with nested case control studies. The function's arguments are the same as for the main smcfcs function, except for smformula, set, event and nrisk - see above for details on how these should be specified.

#### Author(s)

```
Ruth Keogh <ruth.keogh@lshtm.ac.uk>
Jonathan Bartlett <jonathan.bartlett1@lshtm.ac.uk>
```

## **Examples**

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smcfcs.parallel

Parallel substantive model compatible imputation

## Description

Runs substantive model compatible imputation using parallel cores

## Usage

```
smcfcs.parallel(
  smcfcs_func = "smcfcs",
  seed = NULL,
  m = 5,
  n_cores = parallel::detectCores() - 1,
  cl_type = "PSOCK",
  outfile = "",
   ...
)
```

#### **Arguments**

smcfcs_func	Specifies which base smcfcs function to call. Possible values are 'smcfcs', 'smcfcs.casecohort', 'smcfcs.dtasam', 'smcfcs.nestedcc'. Defaults to 'smcfcs'.
seed	Optional seed, set as 'set.seed' when 'n_cores = 1', or as 'parallel::clusterSetRNGStream' when 'n_cores $>$ 1'.
m	Number of imputed datasets to generate.
n_cores	Number of cores over which to split the 'm' imputations. If 'n_cores' is not divisible exactly by 'm', one of the cores will perform more/less imputations that the rest such that the final result still contains 'm' imputed datasets.
cl_type	Either "PSOCK" or "FORK". If running on a Windows system "PSOCK" is recommended, otherwise for Linux/Mac machines "FORK" tends to offer faster computation - see parlmice.
outfile	Optional character path to location for output from the workers. Useful to diagnose rejection sampling warnings. File path must be formulated as "path/to/filename.txt".
• • •	Additional arguments to pass on to smcfcs, smcfcs.casecohort, smcfcs.dtsam, or smcfcs.nestedcc.

## **Details**

This function can be used to call one of the substantive model compatible imputation methods using parallel cores, to reduce computation time. You must specify the arguments required for the standard smcfcs call, and then specify your the arguments for how to use parallel cores.

## Value

An object of type "smcfcs", as would usually be returned from smcfcs.

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## Author(s)

Edouard F. Bonneville <e.f.bonneville@lumc.nl>
Jonathan Bartlett <jonathan.bartlett1@lshtm.ac.uk>

## **Examples**

```
## Not run:
# Detect number of cores
parallel::detectCores()

imps <- smcfcs.parallel(
    smcfcs_func = "smcfcs",
    seed = 2021,
    n_cores = 2,
    originaldata = smcfcs::ex_compet,
    m = 10,
    smtype = "compet",
    smformula = list(
        "Surv(t, d == 1) ~ x1 + x2",
        "Surv(t, d == 2) ~ x1 + x2"
    ),
    method = c("", "", "norm", "norm")
)

## End(Not run)</pre>
```

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